

Notes on a Java translator from BNs to join-tree Prism programs (version 1.3)

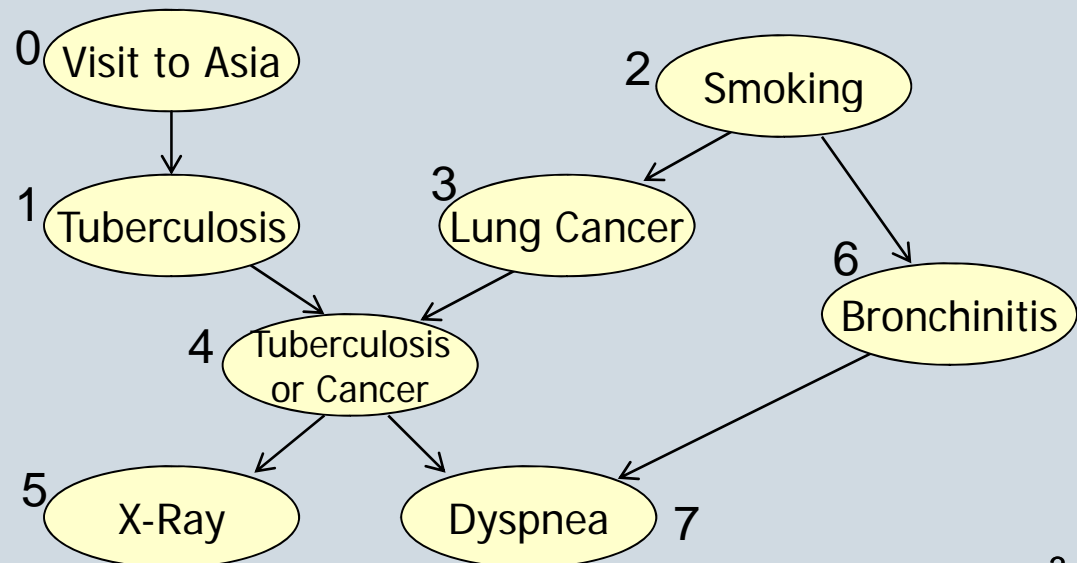
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Background (1 of 3)

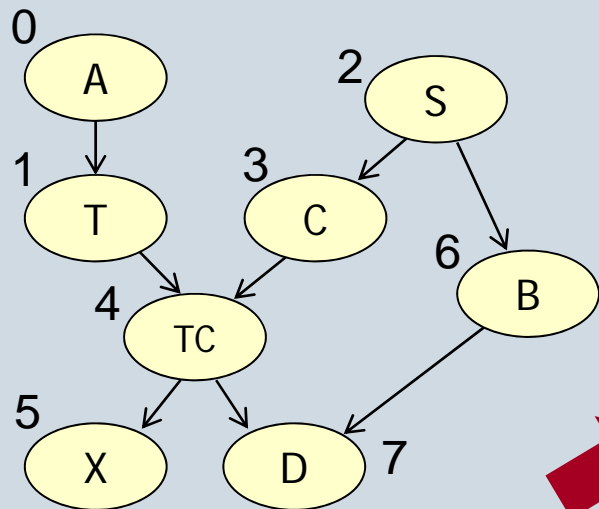
- Translation from BNs to join-tree Prism programs
 1. Construct a join tree (a bucket tree) following [Kask et al. 2005]
 2. Translate the join tree to a Prism program
- This translator is a simplified (less optimized) version of the one used in [Sato & Kameya 2008]
- The theoretical background is given in [Sato 2007] and [Sato & Kameya 2008]
- Running example:
Asia network



Background (2 of 3)

■ Step 1: Building a JT (a bucket tree)

- Determine the order O of variables to be eliminated
 - Minimum deficiency ordering (MDO) [D'Ambrosio 1999] is used by default
- Construct clusters and connect them under O

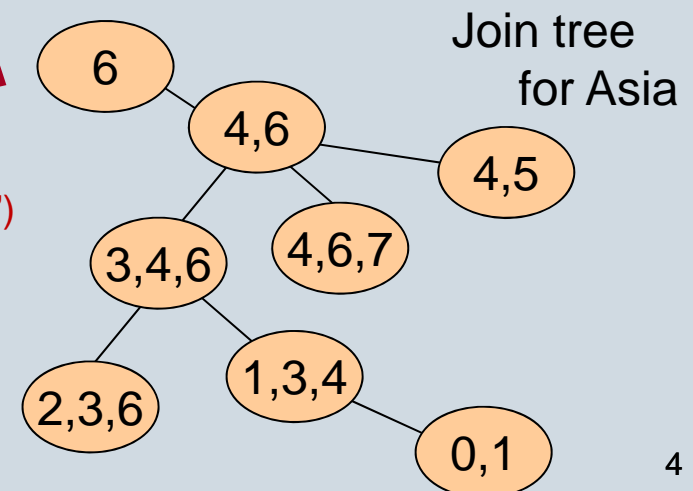


Bucket [0]: { $p(0), p(1|0)$ } → **cl_0(1)**
 Bucket [1]: { $p(4|1,3), \text{cl}_0(1)$ } → $\text{cl}_1(3,4)$
 Bucket [5]: { $p(5|4)$ } → $\text{cl}_5(4)$
 Bucket [7]: { $p(7|4,6)$ } → $\text{cl}_7(4,6)$
 Bucket [2]: { $p(2), p(3|2), p(6|2)$ } → $\text{cl}_2(3,6)$
 Bucket [3]: { $\text{cl}_1(3,4), \text{cl}_2(3,6)$ } → $\text{cl}_3(4,6)$
 Bucket [4]: { $\text{cl}_5(4), \text{cl}_7(4,6), \text{cl}_3(4,6)$ } → $\text{cl}_4(6)$
 Bucket [6]: { $\text{cl}_4(6)$ } → $\text{cl}_6()$

Prob. marginalized with variable 0 ("A")

Bucket [0]: { $p(0), p(1|0)$ }
 Bucket [1]: { $p(4|1,3)$ }
 Bucket [5]: { $p(5|4)$ }
 Bucket [7]: { $p(7|4,6)$ }
 Bucket [2]: { $p(2), p(3|2), p(6|2)$ }
 Bucket [3]: { }
 Bucket [4]: { }
 Bucket [6]: { } (initial)

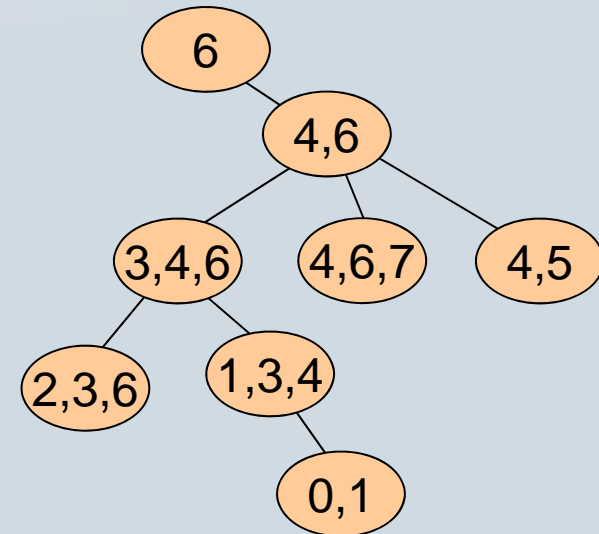
CPT entry for variable 6 ("B")



Background (3 of 3)

■ Step 2: Translate the constructed JT to Prism

Bucket [0]: { $p(0)$, $p(1|0)$ } \rightarrow $cl_0(1)$
Bucket [1]: { $p(4|1,3)$, $cl_0(1)$ } \rightarrow $cl_1(3,4)$
Bucket [5]: { $p(5|4)$ } \rightarrow $cl_5(4)$
Bucket [7]: { $p(7|4,6)$ } \rightarrow $cl_7(4,6)$
Bucket [2]: { $p(2)$, $p(3|2)$, $p(6|2)$ } \rightarrow $cl_2(3,6)$
Bucket [3]: { $cl_1(3,4)$, $cl_2(3,6)$ } \rightarrow $cl_3(4,6)$
Bucket [4]: { $cl_5(4)$, $cl_7(4,6)$, $cl_3(4,6)$ } \rightarrow $cl_4(6)$
Bucket [6]: { $cl_4(6)$ } \rightarrow $cl_6()$



$node_x1(X3,X4) :- pot_x1(X1,X3,X4).$
 $pot_x1(X1,X3,X4) :- node_x0(X1), cpt(x4,[x1=X1,x3=X3],X4).$

$cpt(X,Pa,V) :-$
 ($evidence(X,V)$ -> $msw(bn(X,Pa),V)$
 ; $msw(bn(X,Pa),V)$
).

Prism clauses

How to install the translator

■ Requirements:

- JDK 1.5 or later is installed
 - does not work on JDK 1.4 or earlier
 - Add `$(TOP_DIR)/lib` to CLASSPATH appropriately

■ Procedure:

- Let `$(TOP_DIR)` be the top directory for BN2Prism
- Compile the translator:

```
> cd $(TOP_DIR)/src  
> make
```

Edit Makefile according
to your environment



How to run the translator (1 of 4)

- BN specification files (input):
 - the filename is assumed to be "BASENAME.xml"
(e.g. BASENAME = asia, alarm, etc.)
 - Two format types are available
 - XMLBIF
 - XBIF (used in UAI-06 Evaluation Workshop; just a temporary name in this document)
 - To specify the evidences in XMLBIF, a separate evidence file is required
 - The format needs to follow the XMLBIF-EVIDENCE format
 - In XBIF, on the other hand, the information on evidences is buried in the BN specification file

How to run the translator (2 of 4)

■ Output:

- Translated join-tree Prism program
 - BASENAME.psm
- Translated evidence file (if evidences are given)
 - BASENAME_evid.psm;
- [optional] A file that contains randomly generated evidences
 - BASENAME_revid[0-3].psm
 - BASENAME_revid[0-3].pnl

0 - 0% of all variables (i.e. no evidences)
1 - 25% of all variables
2 - 50% of all variables
3 - 75% of all variables

How to run the translator (3 of 4)

■ Command:

```
> java BN2Prism [-f FORMAT][-o][-t][-r][-e][-z][-n][-v][-h] BASENAME
```

■ Command line options:

- -f FORMAT : the translator reads the input whose format is FORMAT. FORMAT is either xmlbif (for XMLBIF) or xbif (for XBIF)
- -o : the translator reads an external file (named BASENAME.num) that specifies the elimination order.
- -t : the translator reads transposed CPTs (see below).
- -r : the translator assigns random probabilities to the parameters.
- -e : the translator generates auxiliary files that specify the random evidences
- -z : the translator will make zero-compression of CPTs
- -n: the translator normalizes the entries in CPTs
- -v : the translator outputs detailed messages as comments.
- -h : a brief help is displayed.

How to run the translator (4 of 4)

■ Example:

- Assume we have asia.xml (in XMLBIF) and asia_evid.xml (in XMLBIF-EVIDENCE)
- Basic:

`> java BN2Prism -f xmlbif asia` or simply `> java BN2Prism asia`

- When the entries in the CPTs in asia.xml are *transposed*:

`> java BN2Prism -f xmlbif -t asia`

- When asia.xml follows the XBIF (not XMLBIF) format:

`> java BN2Prism -f xbif asia`

How to run the translated Prism program (1 of 3)

- Three types of model description are generated:
 - For belief propagation on JT (world/0-1)
 - *As described before*
 - For naïve probability computation (world_n/0-1)

```
world_n(Es):- assert_evidence(Es),!,world_n.  
world_n:- world_n(_,_,_,_,_,_,_,_).
```

```
world_n(X0,X1,X2,X3,X4,X5,X6,X7) :-  
  cpt(x0,[],X0), cpt(x1,[x0=X0],X1), cpt(x2,[],X2), cpt(x3,[x2=X2],X3), cpt(x4,[x1=X1,x3=X3],X4),  
  cpt(x5,[x4=X4],X5), cpt(x6,[x2=X2],X6), cpt(x7,[x4=X4,x6=X6],X7).
```

- For sampling (world_s/1)

```
world_s([x0=X0,x1=X1,x2=X2,x3=X3,x4=X4,x5=X5,x6=X6,x7=X7]):-  
  msw(bn(x0,[],X0), msw(bn(x1,[x0=X0],X1), msw(bn(x2,[],X2),  
  msw(bn(x3,[x2=X2],X3), msw(bn(x4,[x1=X1,x3=X3],X4), msw(bn(x5,[x4=X4],X5),  
  msw(bn(x6,[x2=X2],X6), msw(bn(x7,[x4=X4,x6=X6],X7)).
```

How to run the translated Prism program (2 of 3)

- Load the program ($\$(TOP_DIR)/includes/bn_common.psm$ needs to be copied to the current working directory in advance):

```
?- prism(asia).
```

- Check the distribution on each variable:

```
?- check_j_dist.  
?- check_n_dist.  
?- check_dist.
```

← BP on JT

← Naïve style

← Both styles

[Note]

Naïve style takes exponential time!

- Give an evidence list to `check_dist/1`, `check_j_dist/1`, `check_n_dist/1` for computing conditional distributions:

```
?- check_j_dist([x3=v3_0]).  
?- check_n_dist([x5=v5_1]).  
?- check_dist([x3=v3_0,x5=v5_1]).
```

[Note]

x3 refers to the 4th variable (*Cancer*)
v3_0 refers to the 1st value (*Present*)
of the 4th variable (*Cancer*)

Probability computation above is made by
"hindsight" computation provided since Prism 1.9

How to run the translated Prism program (3 of 3)

■ Batch execution:

```
> upprism BASENAME [Evid1 Evid2 ....]
```

- Prism system does the followings for each *Evid1, Evid2,*
 - Read an evidence list *Es* from *EvidN*
 - Run `check_j_dist(Es)`
- Example:

```
> upprism asia asia_evid.psm asia_revid0.psm asia_revid1.psm
```

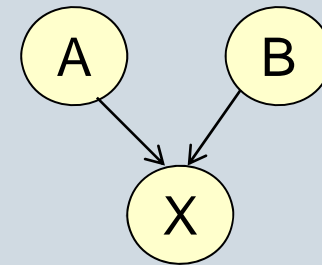
Note: Handling evidences

- In the PRISM program generated by BN2Prism, for each evidence $X=V$, `evidence(X,V)` will be added into the Prolog database, before probabilistic inferences performed
- Instead of calling `msw/2` directly, we call a wrapper predicate `cpt/3` that checks the existence of a evidence:

```
cpt(X,Pa,V):-  
  ( evidence(X,V) -> msw(bn(X,Pa),V)  
                                     % use only the value of the evidence if it exists  
  ; msw(bn(X,Pa),V)                 % otherwise, choose a value from possible ones  
  ).
```

Note: Compressing CPT entries with zero probability

- If an entry in a CPT for a variable X has zero probability, we wish to remove such an entry to reduce the search space
- In other words, we change the set of outcomes of X according to the context (an instantiation of parent nodes A and B)
 - X takes on $\{0, 1\}$ when $B = 1$
 - X takes on $\{1\}$ when $A = 0$ and $B = 0$
 - X takes on $\{0\}$ when $A = 1$ and $B = 0$
- In PRISM programs, this can be realized with more fine-grained ‘values’ declarations
 - One computational advantage of logical (propositional) approaches



A	B	X	P(X A,B)
0	0	0	0.0
0	0	1	1.0
0	1	0	0.7
0	1	1	0.3
1	0	0	1.0
1	0	1	0.0
1	1	0	0.4
1	1	1	0.6

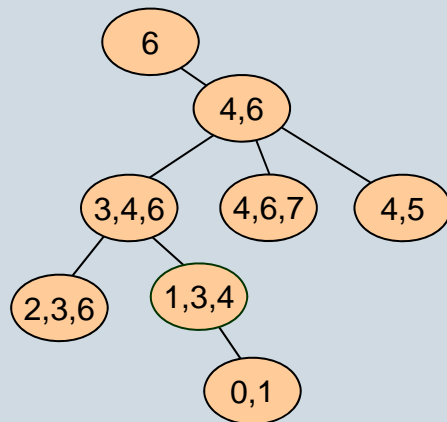
Note: Input/output dependencies in a bucket (1 of 3)

- Literals in the clause body are ordered according to the input/output dependencies among the probabilistic predicates

Add Input/output modes:

Bucket [0]: { $p(-0)$, $p(-1|+0)$ } \rightarrow $cl_0(-1)$
Bucket [1]: { $p(-4|+1,+3)$, $cl_0(-1)$ } \rightarrow $cl_1(+3,-4)$
Bucket [5]: { $p(-5|+4)$ } \rightarrow $cl_5(+4)$
Bucket [7]: { $p(-7|+4,+6)$ } \rightarrow $cl_7(+4,+6)$
Bucket [2]: { $p(-2)$, $p(-3|+2)$, $p(-6|+2)$ } \rightarrow $cl_2(-3,-6)$
Bucket [3]: { $cl_1(+3,-4)$, $cl_2(-3,-6)$ } \rightarrow $cl_3(-4,-6)$
Bucket [4]: { $cl_5(+4)$, $cl_7(+4,+6)$, $cl_3(-4,-6)$ } \rightarrow $cl_4(-6)$
Bucket [6]: { $cl_4(-6)$ } \rightarrow $cl_6()$

Order the elements in a bucket (left-to-right) according to the input/output dependencies

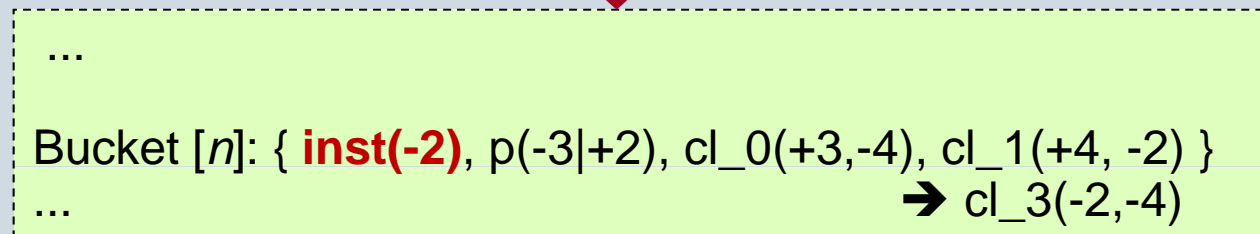
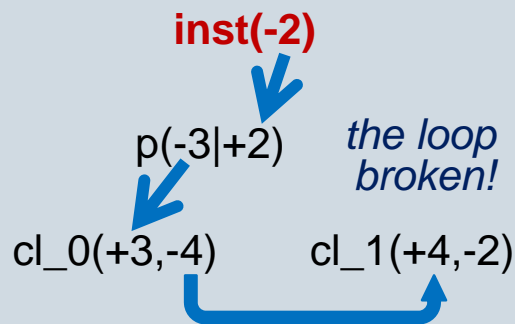
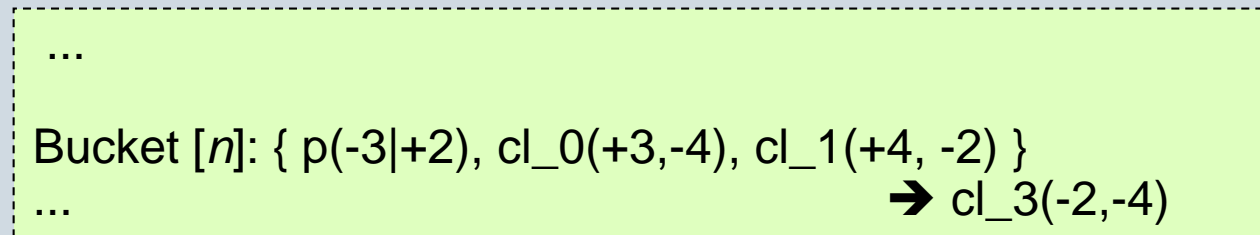
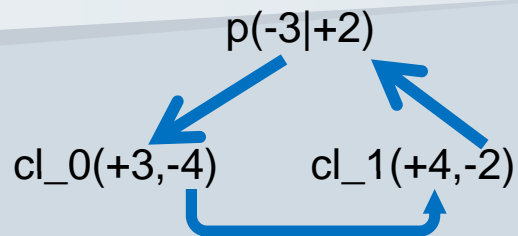


Bucket [0]: { $p(-0)$, $p(-1|+0)$ } \rightarrow $cl_0(-1)$
Bucket [1]: { $cl_0(-1)$, $p(-4|+1,+3)$ } \rightarrow $cl_1(+3,-4)$
Bucket [5]: { $p(-5|+4)$ } \rightarrow $cl_5(+4)$
Bucket [7]: { $p(-7|+4,+6)$ } \rightarrow $cl_7(+4,+6)$
Bucket [2]: { $p(-2)$, $p(-3|+2)$, $p(-6|+2)$ } \rightarrow $cl_2(-3,-6)$
Bucket [3]: { $cl_2(-3,-6)$, $cl_1(+3,-4)$ } \rightarrow $cl_3(-4,-6)$
Bucket [4]: { $cl_3(-4,-6)$, $cl_5(+4)$, $cl_7(+4,+6)$ } \rightarrow $cl_4(-6)$
Bucket [6]: { $cl_4(-6)$ } \rightarrow $cl_6()$

$node_x1(X3,X4) :- pot_x1(X1,X3,X4).$
 $pot_x1(X1,X3,X4) :- node_x0(X1), cpt(x4,[x1=X1,x3=X3],X4).$

Note: Input/output dependencies in a bucket (2 of 3)

- Sometimes we have a loop of dependency in a bucket
- We insert some “instanciate” literals to break such a loop




```
node_x3(X2,X4) :- pot_x3(X2,X3,X4).
pot_x3(X2,X3,X4) :-
    instanciate(x2,X2), cpt(x3,[x2=X2],X3), node_x0(X3,X4), node_x1(X4,X2).

instanciate(X,V) :- % forcedly instanciate variable X as V
    range(X,Values), (evidence(X,V) -> true ; member(V,Values)).
```

Note: Input/output dependencies in a bucket (3 of 3)

- Unfortunately, the “instanciate” predicates cannot exploit the context-specific information (and hence cannot compress the CPT entries with zero probability)
- As a side effect, we can give the mode declarations to the probabilistic predicates:

```
Bucket [0]: { p(-0), p(-1|+0) } → cl_0(-1)
Bucket [1]: { cl_0(-1), p(-4|+1,+3) } → cl_1(+3,-4)
Bucket [5]: { p(-5|+4) } → cl_5(+4)
Bucket [7]: { p(-7|+4,+6) } → cl_7(+4,+6)
Bucket [2]: { p(-2), p(-3|+2), p(-6|+2) } → cl_2(-3,-6)
Bucket [3]: { cl_2(-3,-6), cl_1(+3,-4) } → cl_3(-4,-6)
Bucket [4]: { cl_3(-4,-6), cl_5(+4), cl_7(+4,+6) } → cl_4(-6)
Bucket [6]: { cl_4(-6) } → cl_6()
```



```
:- mode node_x0(-).
:- mode node_x1(+,-).
:- mode node_x5(+).
...

:- mode pot_x0(-,-).
:- mode pot_x1(-,+,-).
:- mode pot_x5(+,-).
...
```

Note: File format of network specification

- In both XMLBIF and XBIF, CPTs are specified in `<TABLE>...</TABLE>`
 - There can be different orders of entries (conditional probabilities or parameters) in a CPT.
 - Basically the translator assumes the order illustrated in <http://www.cs.cmu.edu/afs/cs/user/fgcozman/www/Research/InterchangeFormat/> :

```
<TABLE>0.9 0.1 0.7 0.3 0.8 0.2 0.4 0.6</TABLE>
```

- On the other hand, some network files adopt a *transposed* order:

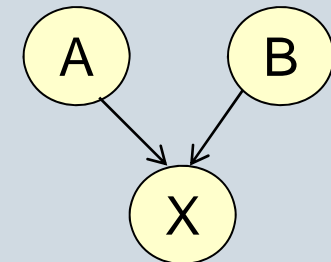
```
<TABLE>0.9 0.7 0.8 0.4 0.1 0.3 0.2 0.6</TABLE>
```

- BN2Prism accepts the transposed CPTs when the `-t` option is specified.
- Furthermore, with the `-n` option, the CPT entries will be normalized inside the translator:

```
<TABLE>1.0 3.0 1.0 1.0 2.0 1.0 2.0 0.5</TABLE>
```



```
<TABLE>0.25 0.75 0.5 0.5 0.666666 0.333333 0.8 0.2</TABLE>
```



A	B	X	P(X A,B)
0	0	0	0.9
0	0	1	0.1
0	1	0	0.7
0	1	1	0.3
1	0	0	0.8
1	0	1	0.2
1	1	0	0.4
1	1	1	0.6

References

- [D'Ambrosio 1999]
B. D'Ambrosio (1999). Inference in Bayesian networks. *AI Magazine* 20 (2), pp.21-36.
- [Kask et al. 2005]
K. Kask, R. Dechter, J. Larrosa and A. Dechter (2005). Unifying tree decompositions for reasoning in graphical models. *Artificial Intelligence* 166 (1-2), pp.165-193.
- [Sato 2007]
T. Sato (2007). Inside-outside probability computation for belief propagation. *Proceedings of the 20th International Joint Conference on Artificial Intelligence (IJCAI-2007)*, pp.2605–2610, 2007.
- [Sato and Kameya 2008]
T. Sato and Y. Kameya (2008). New advances in logic-based probabilistic modeling by PRISM. In De Raedt et al. (editors), *Probabilistic Inductive Logic Programming*, LNCS 4911, Springer, pp.118–155, 2008.